# **Research Papers**

# An Approach to Design Broadband Air Backed Piezoelectric Sensor

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In this work, an approach to the design of broadband thickness-mode piezoelectric transducer is presented. In this approach, simulation of discrete time model of the impulse response of matched and backed piezoelectric transducer is used to design high sensitivity, broad bandwidth, and short-duration impulse response transducers. The effect of matching the performance of transmitting and receiving air backed PZT-5A transducer working into water load is studied. The optimum acoustical characteristics of the quarter wavelength matching layers are determined by a compromise between sensitivity and pulse duration. The thickness of bonding layers is smaller than that of the quarter wavelength matching layers so that they do not change the resonance peak significantly. Our calculations show that the -3 dB air backed transducer bandwidth can be improved considerably by using quarter wavelength matching layers. The computer model developed in this work to predict the behavior of multilayer structures driven by a transient waveform agrees well with measured results. Furthermore, the advantage of this this model over other approaches is that the time signal for optimum set of matching layers can be predicted rapidly.

Keywords: piezoelectric, equivalent circuits, impulse response, frequency response, matching layers, z-transform.

### 1. Introduction

In ultrasonic broadband applications such as medical imaging or non-destructive testing piezoelectric transducers should generate/receive ultrasonic signals with good efficiency over a large frequency range. This requires the use of broadband piezoelectric transducer with high sensitivity and short-duration impulse response. Piezoelectric ceramic transducers usually have a specific acoustic impedance much greater than those of the usual load present in diagnostic ultrasound ones. This impedance difference generates ultrasonic pulses of pulse width much larger than electric signals. For reducing the multiple internal reflections, front impedance matching layers between piezoelectric transducer and load medium are required (BEERMAN, 1981; PERSSON et al., 1985; TODA et al., 2010). Several theoretical models for calculating the optimum acoustic impedance for the front matching layers are reported in the literature (SHUNG et al., 2007; KAZYS et al., 2006). The acoustic backing material is used at the back of the transducer for damping the free oscillation. However, these materials absorb acoustic energy and therefore reduce the transducer sensitivity (KONOVALOV, 2002). The effect of air backing on receiving sensitivity for piezoelectric micro-machined hydrophone was investigated (LEE et al., 2010). MUL-HOLLAND et al. (2008) developed a linear system model for a composite piezoelectric transducer with multiple matching layers. The transmission line model is widely used for designing efficient broad band air backed piezoelectric transducers. The transmission line model is normally Fourier transform representation of the piezoelectric transducer and therefore yields solutions in terms of angular frequency. Researchers (DESILETS) et al., 1978; LEWIS, 1980; CHEN, 2010) typically use frequency domain equivalent circuits and derive the time domain transient response by inverse fast Fourier transform (FFT). The mathematical treatment is complicated when more than two layers are considered and the technique is restricted to certain excitations. Transformations of the transducer equivalent circuit in discrete time domain was described by (ESTANBOULI et al., 2006) and (KAZYS et al., 1977).

This work presents a more complete model for predicting the behavior of a multilayered piezoelectric transducer. It uses z-transform techniques to provide a discrete time implementation of the original frequency domain circuit of Mason (BERLINCOURT *et al.*, 1964; KAZYS, 1978). The optimum acoustical characteristics of the matching layers are determined by defining a compromise between the sensitivity and the duration time of the impulse response. Also the effect of bonding layers on the resonance frequency of a transducer is studied.

#### 2. Transducer equivalent circuits

Transducer performs the conversion of electrical energy into mechanical energy and vise verse (ALI et al., 2012). There is a fundamental relationship between the properties of the transducer and the quality of the resulting image; a several techniques have been developed for modelling transducer behaviour and hence predicting the required system response. Many computer models that describe the behaviour of ultrasonic piezoelectric transducer are currently available (YAACOB et al., 2011; SHERRITY et al., 1997; TODA et al., 2012). In this paper a simulation is applied using the developed computer model (ALI, 1999) to evaluate the discrete time response. The computer model is split into two parts. First, the basic transfer function of the loaded piezoelectric element is evaluated in discrete form using the Z-transform technique. Second, the discrete time responses obtained in that way are processed by a nested set of digital filter operations that simulate the reverberation in the coupling lavers connected to the transducer and the backing and medium load.

The three required transfer functions of the transducer depicted in Fig. 1 are: a voltage transfer function relating the excitation voltage  $(V_s)$  to the voltage developed across the transducer terminals (V); a transmit transfer function relating the force generated  $(F_0)$ to a voltage excitation  $(V_s)$ ; and a receiver transfer function relating the force incident on the transducer front face  $(F_i)$  to the voltage developed across the transducer terminals (V). The basis for the development of the expression for the above transfer functions is a generalization of the circuit of Fig. 1. The generalized circuit depicted in Fig. 2 will allow the simple derivation of the transfer function. From this circuit particularly simple transfer functions and impedances can be expressed as described below:

$$\frac{V}{V_s} = \frac{sC_0R_M - \phi^2}{sC_0[1 + sC_0R_s]R_M - \phi^2},$$
(1)

$$\frac{V_{RM}}{V_s} = \frac{sC_0R_M}{sC_0[1+sC_0R_s]R_M - \phi^2},$$
 (2)

$$\frac{V}{V_M} = \frac{sC_0R_M}{sC_0[1+sC_0R_s]Z_A - \phi^2},$$
 (3)

$$R_s = \frac{sC_0[1 + sC_0R_s]Z_A - \phi^2}{sC_0[1 + sC_0R_s]Z_A}.$$
 (4)



Fig. 1. Equivalent circuit of the piezoelectric transducer:  $V_s$  excitation voltage;  $C_0$  static capacitance of the piezoelectric element;  $\phi$  electrical to mechanical conversion factor;  $Z_A$ ,  $Z_B$  distributed components of the familiar 'T' equivalent circuit of a transmission line;  $Z_r$ ,  $Z_s$  acoustic impedance of the materials in contact with the front and back face of the piezoelectric element;  $F_0$  transmitted force;  $F_i$  received force; and V voltage seen across the terminals of the transducer.



Fig. 2. Simplified general circuit.  $R_M$  represents two impedance.

For the case of no incident force on the face of the transducer, from Fig. 1,  $R_M$  is seen to be the impedance looking into center tapped transmission line terminated by distributing impedances  $Z_r$  and  $Z_s$ . This is shown in Fig. 3, from which it can be seen that:

$$R_m = \frac{2Z_A Z_B + Z_B^2 + (Z_A + Z_B)(Z_r + Z_s) + Z_r Z_s}{2Z_B + Z_r + Z_s}.$$
 (5)

In Fig. 1  $Z_A$  and  $Z_B$  represent the distributed components of the familiar T equivalent circuit of a transmission line. However, in this case  $Z_A$  and  $Z_B$  have a mechanical interpretation:

$$Z_A = \frac{2Z_C}{e^{sX/V} - e^{-sX/V}} \tag{6}$$



Fig. 3. The equivalent circuit of the impedance  $R_M$  which is that looking into a center tapped transmission line terminated with impedance  $Z_r$  and  $Z_s$ .

and

$$Z_B = Z_C \frac{1 - e^{-sX/V}}{1 + e^{-sX/V}},$$
(7)

where  $Z_C$  is the acoustic impedance of the piezoelectric element and V is the velocity of compression waves in the piezoelectric material. The term  $X/V = T_P$  represents the time delay for an acoustic wave to propagate from one face of the piezoelectric element to the other. It is clear that a number of discrete time intervals can approximately represent the time delay  $T_P = m_0 T$ , where  $m_0$  is an integer and T is the sampling period. OPPENHEIM et al. (1975) and JURY (1964) discussed the properties of z-transform and its relationship to the Fourier and Laplace transform. In terms of the Laplace transform, the time delay  $\exp(-sX/V)$  approximates to  $\exp(-sm_0T) = z^{-m_0}$ , where the substitution  $z = \exp(sT)$  has been made and the approximate time delay is given in terms of the z-transform. The impedance of  $R_M$ ,  $Z_r$ ,  $Z_s$ , and  $R_s$  can be presented as polynomial quotient expression:

$$R_{M} = \frac{R_{M \text{num}}}{R_{M \text{den}}}, \qquad Z_{r} = \frac{Z_{r \text{num}}}{Z_{r \text{den}}},$$

$$Z_{s} = \frac{Z_{s \text{num}}}{Z_{s \text{den}}}, \qquad R_{s} = \frac{R_{s \text{num}}}{R_{s \text{den}}}.$$
(8)

#### 2.1. The voltage response (voltage-voltage)

Substituting the above expression into Eq. (1) produces the full expression for the voltage transfer function:

$$V = \frac{V_s R_{sden} [s C_0 R_{Mnum} - \phi^2 R_{Mden}]}{s C_0 [R_{sden} + s C_0 R_{snum}] R_{Mnum} - \phi^2 R_{Mden}}.$$
 (9)

# 2.2. The transmit response (voltage-force)

The calculation of transmission and reception transfer functions involves a two-step procedure. For the transmit response, first the response at the point labeled  $V_2$  in Figs. 1 and 3 is obtained. Next the transmitted force across the matching layers is calculated from the response at  $V_2$ . From Fig. 3 it can be deduced that

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$$10V_s = \frac{[Z_B^2 + Z_B(Z_r + Z_s) + Z_r Z_s]V_{RM}}{a^*}$$
(10)

where

$$a^* = 2Z_A Z_B + Z_B^2 + (Z_A + Z_B)(Z_{RF} + Z_{RB}) + Z_{RF} Z_{RB},$$

where  $Z_{RB}$  and  $Z_{RF}$  are terminating impedances at the back and front of the transducer assembly respectively, that is the material of infinite length. From Eq. (2), Eq. (10) becomes

$$V_2 = \frac{s\phi C_0[Z_B^2 + Z_B(Z_r + Z_s) + Z_r Z_s]V_s}{b^*}, \quad (11)$$

where

$$b^* = sC_0[1 + sC_0R_s][2Z_AZ_B + Z_B^2 + (Z_AZ_B)(Z_r + Z_s) + Z_rZ_s] - \phi^2[2Z_B + Z_r + Z_s].$$

In this work, using four matching layers and the transfer of force through these layers (ALI, 1999) from piezoelectric element of impedance  $Z_c$  to an impedance  $Z_r$ , the final expression for the transmit response can be obtained by substituting Eqs. (6) and (7) into Eq. (11) and rearranging. It can be shown that:

$$F_0 = \frac{c^*}{2[1 + Ar_0 z^{-m_0} + (r_0 + z^{-m_0} B]]},$$
 (12)

where

$$c^* = V_2[1 + (1 + r_1)(1 + r_2)(1 + r_3) \cdot (1 + r_4)z^{-(m_0 + m_1 + m_2 + m_3 + m_4)}]$$

where A and B are functions of the reflection coefficients  $(r_0, r_1, r_2, r_3, r_4)$  referring to the interface between the layers;  $m_0, m_1, m_2, m_3, m_4$  integer numbers (ALI, 1999).

#### 2.3. The receiver response (force-voltage)

Upon reception, the force transfer across an arbitrary number of matching layers has to be calculated. This involves the impedance of far side of the last layer being that of the impedance looking into the transducer from the front face of the piezoelectric element,  $Z_{eq}$  as shown in Fig. 1. From Fig. 1 and Eq. (4)  $Z_{eq}$  can be written as:

$$Z_{eq} = \frac{d^*}{sC_0[1 + sC_0R_s][Z_A Z_B + Z_s] - \phi^2},$$
 (13)

where

$$d^* = sC_0[1 + sC_0R_s][2Z_aZ_B + Z_B^2 + Z_s[Z_A + Z_B]] - \phi^2[Z_s + 2Z_B].$$

Substituting Eqs. (6) and (7) into Eq. (13) and quotient form of  $Z_s$  and may be written as:

$$Z_{eq} = \frac{Z_{eqnum}}{Z_{eqden}}.$$
 (14)

With the reflection coefficients arranged to calculate force transfer in the opposite direction to that defined previously and the last reflection coefficient for the fourth matching layer,  $r_4$  is defined as  $r_4 = (Z_{eq} + Z_1)/(Z_{eq} - Z_1)$ . The response in terms of the incident force  $F_i$  can be calculated as:

$$F_i = \frac{e^*}{a(A+r_0B)},$$
 (15)

where

$$e^* = 2F_i Z_{eqnum} (1+r_0)(1+r_1)$$
  
 
$$\cdot (1+r_2)(1+r_3) z^{-(m_1+m_2+m_3+m_4)}.$$

From Fig. 1. and Fig. 2. a simplified circuit can be used to obtain the voltage  $V_M$ , as shown in Fig. 4, as a function of  $F'_i$ . In this figure Rs is given by Eq. (4) and using Eq. (3) the force-voltage transfer function can be written as

$$V = \frac{F'_{i} s \phi C_{0} R_{\text{num}} (1 - z^{-m_{0}}) \cdot f^{*}}{Z_{eqnum}}, \qquad (16)$$

where

$$f^* = [Z_c Z_{sden}(1 - z^{m_0}) + Z_{snum}(1 + z^{-m_0})].$$



Fig. 4. Simplified circuit used for the calculation of  $V_M$  (Fig. 2) in terms of the force face of the piezoelectric element  $F'_i$ .

For Eqs. (9), (12), (15), and (16) to be fully represented in terms of discrete time, a discrete approximation to the Laplace variables has to be incorporated into this expression. The transfer equation can be solved as a recursive digital filter and these equations can be easily implemented using polynomial algebra routines.

### 3. Results

The simulation is applied using typical transducer data constructed with a lead zirconate titanate (PZT-5A) piezoelectric element (BERLINCOURT et al., 1964) with a different quarter-wave length matching layers. The transmitter response is obtained for a 10-mmdiameter pulse-echo transducer of 5 MHz center frequency and radiating into water medium. The transducer diameter (10 mm) is much greater than its thickness (0.435 mm). As a result, it fulfills the requirement of a 1D transducer model. Figure 5 shows the expected waveform of an air backed transducer when the device acts as a receiver with no matching layer. Once the impulse response is obtained, a fast Fourier transform is performed on the data. Figure 6 shows the pulseecho transducer frequency response. From this figure, it can be seen that the backing layer of air yield -3 dBbandwidth of 0.31 of the central frequency. Let us now examine changes in the performance of transducer with one, two and three quarter wavelength matching layers. Varying each of the matching layers of practical



Fig. 5. The pulse-echo transducer response with no matching layer operating into water load and air backing.



Fig. 6. Pulse-echo transducer frequency response for Fig. 5.

materials enables us to determine the optimum combination of layers/materials that gives a wide bandwidth. The optimized impedance formula is given by (GOLL *et al.*, 1975):

$$\ln\left[\frac{Z_{n+1}}{Z_n}\right] = 2^{-N} \frac{N!}{(N-n)!n!} \ln\left[\frac{Z_{RF}}{Z_0}\right], \qquad (17)$$

where  $Z_n$  is the *n*-matching layer impedance, N is the total number of matching layers,  $Z_0$  is the acoustic impedance of the piezoelectric material, and  $Z_{RF}$  is the acoustic impedance of the load medium (water). The sensitivity was defined as the maximum height of the received pulse, given in terms of volts. Using the matching layer of practical material values reported in Table 1, the sensitivity and bandwidth for the single quarter-wave length matching layer was reported in Fig. 7. It is clear that the sensitivity is maximized and duration pulse is minimized when the matching layer is Glassbeads (SOUQUET et al., 1979). Table 2 shows the optimum parameters for materials used for one, two, and three matching layers. Figure 8 shows the expected waveform at the transducer terminals when the device acts as a receiver with one, two, and three matching layers of air backed transducer. Figure 9 shows the pulse-echo frequency responses for zero, one, two, and three matching layers. It is clear from this figure that the matching layers of one, two, and three layers yield -3 dB bandwidths of 0.54, 1.1 and 1.4 of the center



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Fig. 7. Dependence of sensitivity and duration pulse on the first matching layer.

frequency, respectively and the results are consistent with Eq. (17).

For bonding ceramics, it is common practice to use epoxy resins, such as Araldite, which has very low impedance compared with ceramics. Therefore, if the bond is insufficiently thin, there will be an impedance mismatch at the ceramic interface, causing degradation of transducer performance. SILK *et al.* (1983) showed that an Araldite bond between ceramics and a high impedance backing must have a thickness of less than

Material for quarter wave length	Sensitivity [Volt]	Pulse duration [µs]	Impedance $(Z)$ [Kg/m <sup>2</sup> .s]×10 <sup>6</sup>
Mathylplaten	1.85	4.9	1.1
Polystyrene	2.5	4.7	1.3
Polymethylmeth-acrylate	3.2	3.14	1.5
Glassbeads and Epoxy	4.0	2.44	1.7
Glassbeads-Epoxy [16]	4.2	1.25	1.9
Melopas	4.93	2.6	1.6
AL-Epoxy	5.5	3.1	1.4
Tungsten-araldite	7.0	3.89	1.2
Glass arsenic trisulphide	8.0	4.25	1.1
Tungsten-Epoxy	10.0	4.5	1.0

Table 1. Variety of single matching layer with pulse duration and sensitivity.

Table 2. The optimum value of single, two and three matching layers as a function of sensitivity and duration pulse.

Material for quarter wavelength		Impedance $(Z)$ [Kg/m <sup>2</sup> .s]×10 <sup>6</sup>	Acoustic velocity [m/s]	Pulse duration [µs]	Sensitivity [Volt]
One matching layer	Glassbeads and Epoxy	4.2	2300	1.25	1.9
Two matching layers	Glass arsenic trisulphide	8.0	3000	0.8	2.1
	Polystyrene	2.5	2550	0.0	
Three matching layers	Glass	14.6	5943		
	Glassbeads and Epoxy	4.2	1900	0.7	2.4
	Methyl-platen	1.85	970		



Fig. 8. The pulse-echo transducer responses with single, two and three matching layers operating into water load. These three curves are shifted to emphasize the effect on duration of the signal.



Fig. 9. Amplitude frequency spectrum for one, two and three matching layers and without matching layer.

 $\lambda/200$  to avoid adverse effects. At 5 MHz this corresponds to  $10 \ \mu m$  which can be used as an indication of the required bond thickness. Figure 10 shows the frequency response for three matching layers with  $10 \ \mu m$ bond-lines as compared to that of an idealized device with no bond materials. It can be seen that the bonding material thickness has very little effect on the frequency response. The -3 dB bandwidth drops from 1.4 to 1.3. The backing layer is required when the performance of the front matching layers is nonideal, which is often the case because of limitations in available materials. Resonance is formed by the reflection from front and back face. If reflections from the front face are zero as a result of the use of an ideal front matching layer, performance is improved because resonance cannot be formed solely from reflections from the back boundary



Fig. 10. Amplitude frequency spectrum of three matching layers with bondlines and no bondlines.

(ALI, 2000). Figure 11 shows the frequency response of the three matching layers with back matching layer of copper. The -3 dB bandwidth increases from 1.4 to 1.48.



Fig. 11. Effect of backing one layer of copper as backing with three front matching layers.

MULHOLLAND *et al.* (2008) recorded impulse frequency response for 1 MHz probe with four matching layers as shown in Table 3. The matching layer

Table 3. Materials properties for the experimental multilayer matching scheme (MULHOLLAND *et al.*, 2008).

Material for four matching quarter wavelength	$\begin{array}{c} Impedance \\ [Kg/m^2.s] \times 10^6 \end{array}$	Acoustic velocity [m/s]	
Soda Lime Glass	14.6	5943	
Vitreous Carbon	6.7	4723	
BaSO <sub>4</sub> filled epoxy	2.9	2592	
Epoxy	2.1	1784	



Fig. 12. Experimental transducer frequency response is compared with the proposed model.



Fig. 13. Comparison of the measured and the presented model through transmission impulse response for the four matching layers.

was then attached to the piezoelectric element and attached to a backing block material with an acoustic impedance of 8 MRayls. The pulse-echo impulse response of the transducer was measured in a water tank using a Panametrics 5052PR pulser-receiver to excite the transducer. The echo from a glass block was recorded using a digitizing oscilloscope and was converted to the frequency domain using the FFT. Figure 12 shows the experimental transducer pulse-echo impulse response in the frequency domain (MULHOLLAND et al., 2008) together with presenting modelled response. Figure 13 shows the comparison of the experimental (MULHOLLAND et al., 2008) and the presented model for four matching layers. It is clear that the predicted result is in good agreement with the published experimental data. It is clear from all of these results that calculation using the transducer equivalent circuit proposed in this paper yields an accurate analysis in the design of sensitive short response of air backed transducer.

# 4. Conclusions

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A discrete time model of the thickness mode piezoelectric transducer was used to predict the influence of mechanical layers and intermediate bond lines on the impulse response. The model was obtained from the analysis of the electrical equivalent circuit of a piezoelectric device. The model was implemented directly in the time domain. The optimum acoustic characteristics of the matching layers were determined by defining a compromise between the sensitivity and the pulse duration of impulse response. The effects of bonding layers are smaller so that they do not change the resonance peak significantly. The calculated results show that the  $-3 \, dB$  air backed transducer bandwidth can be improved significantly by using quarter matching layers. The results presented in this paper show that the optimized model predicts measurement results of the received echo waveform and its frequency spectrum. The method has the advantage that the time

signal for an optimum set of matching layers of practical materials can be predicted immediately.

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